

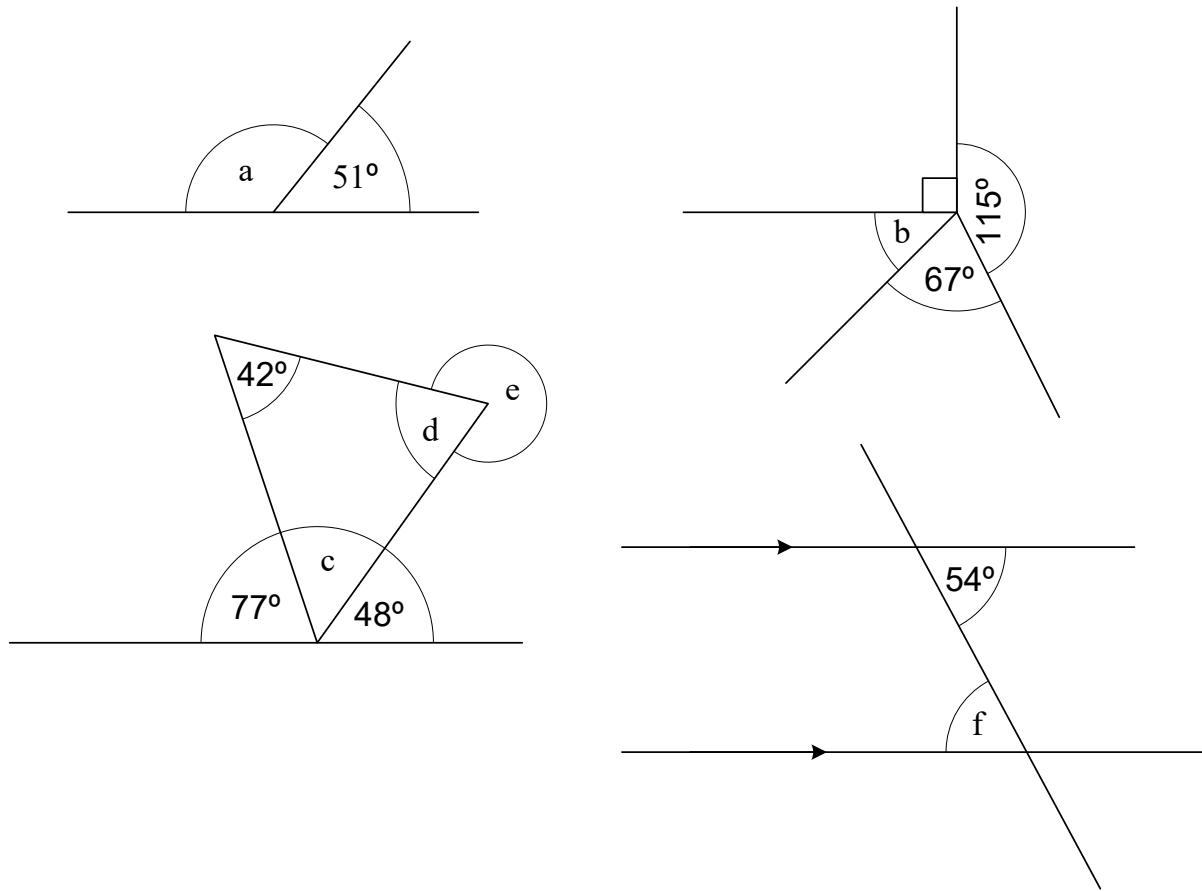
GCSE Mathematics

# Geometric Reasoning

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**Q1** Find the size of the missing angles. Show your reasoning.



a .....

b .....

c .....

d .....

e .....

f .....

**Q2** What type of angle is described below?

a An angle of  $65^\circ$ .

.....

b An angle of  $180^\circ$ .

.....

c An angle of  $145^\circ$ .

.....

d An angle of  $12^\circ$ .

.....

e An angle of  $213^\circ$ .

.....

f An angle of  $90^\circ$ .

.....

g An angle of  $112^\circ$ .

.....

h An angle of  $270^\circ$ .

.....

i An angle of  $94^\circ$ .

.....

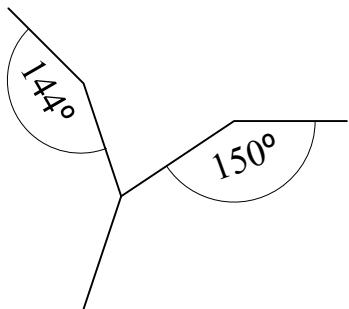
j An angle of  $183^\circ$ .

.....

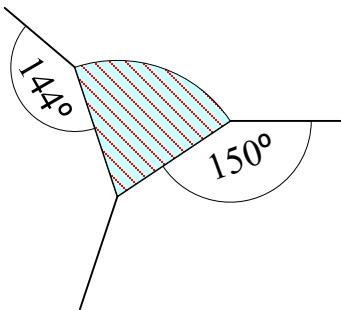
**Q3** The diagram below shows a partial view of two regular polygons.

The length of each side is 2cm.

a Name the shapes. Show how you know.



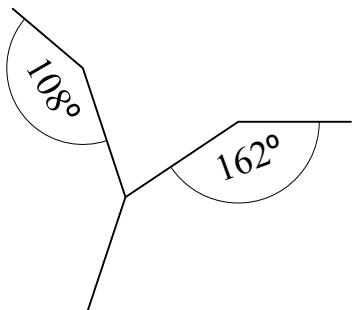
b What is the area of the shaded sector?



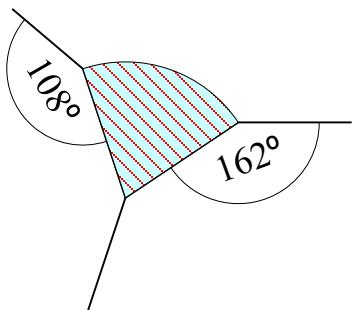
**Q4** Below is a partial diagram of two regular polygons.

The length of each side is 5cm.

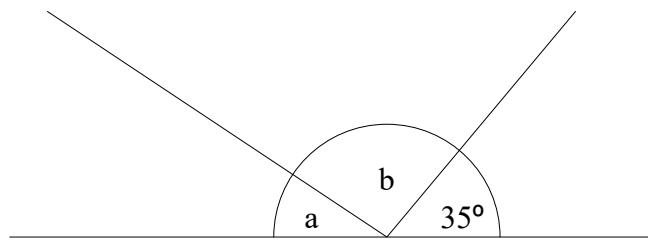
a How many sides has each polygon. Show how you know.



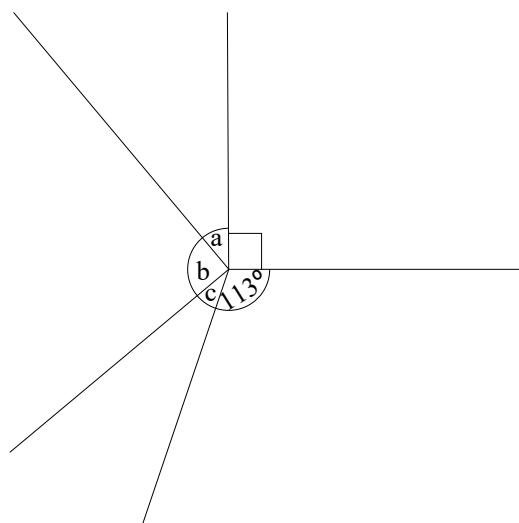
b What is the area of the shaded sector?



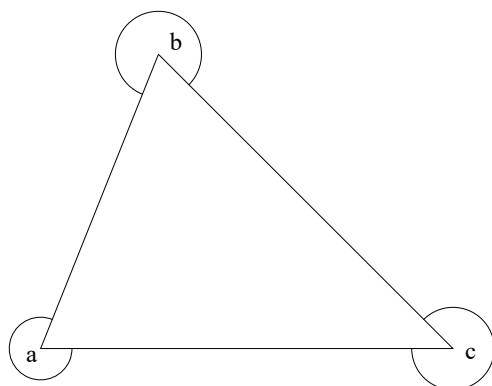
**Q5** Explain why  $a+b=145^\circ$ .



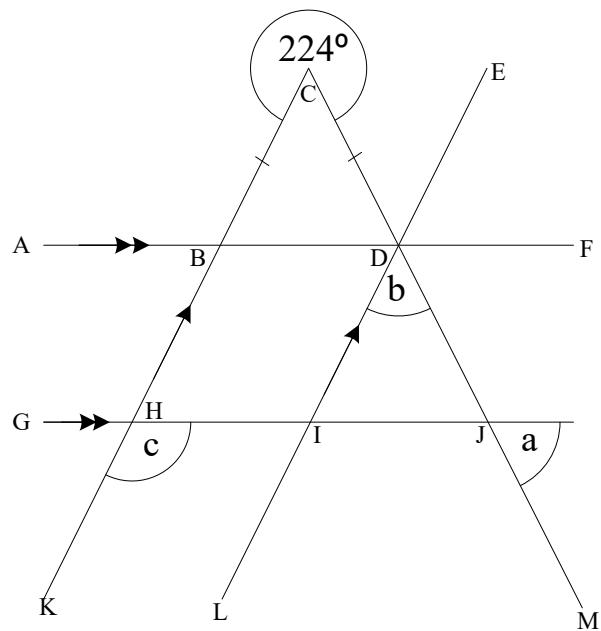
**Q6** Explain why  $a+b+c=157^\circ$



**Q7** Explain why  $a+b+c=900^\circ$



**Q8** Find the values of a, b and c. Give reasons.

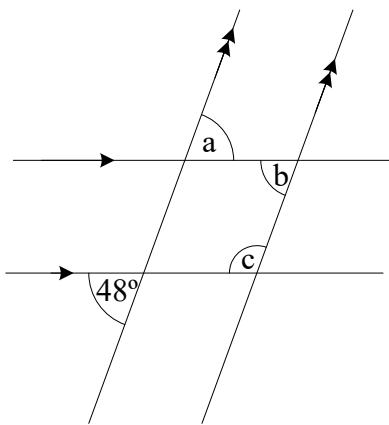


$$a = \dots$$

$$b = \dots$$

$$c = \dots$$

**Q9** Without using, “Angles on a straight line,” explain how angles a, b and c are related to the given angle on the diagram below.



a = .....

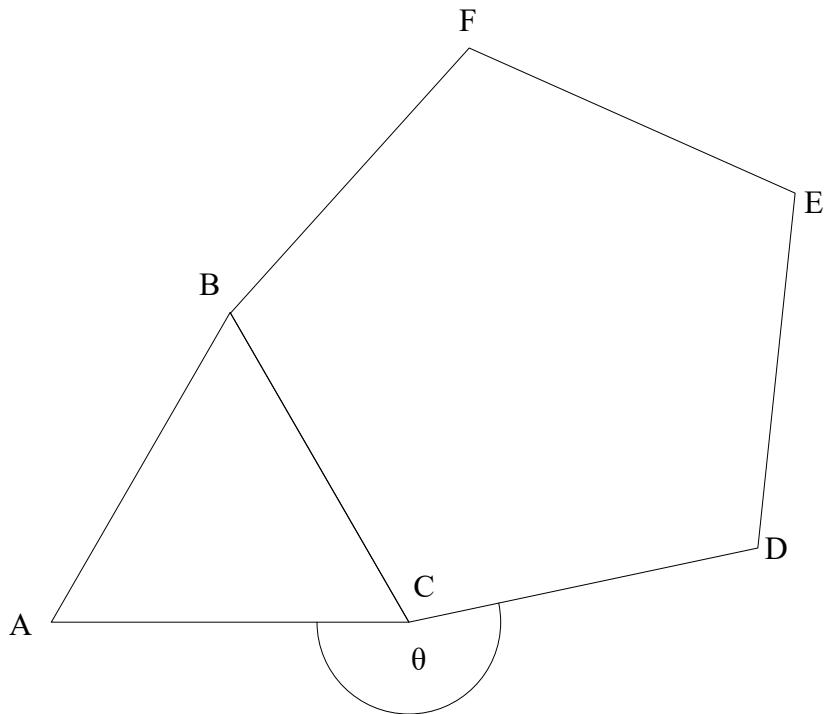
b = .....

c = .....

**Q10** ABC is an equilateral triangle. BCDEF is a regular pentagon.

Find the size of angle  $\theta$ .

Show your working.

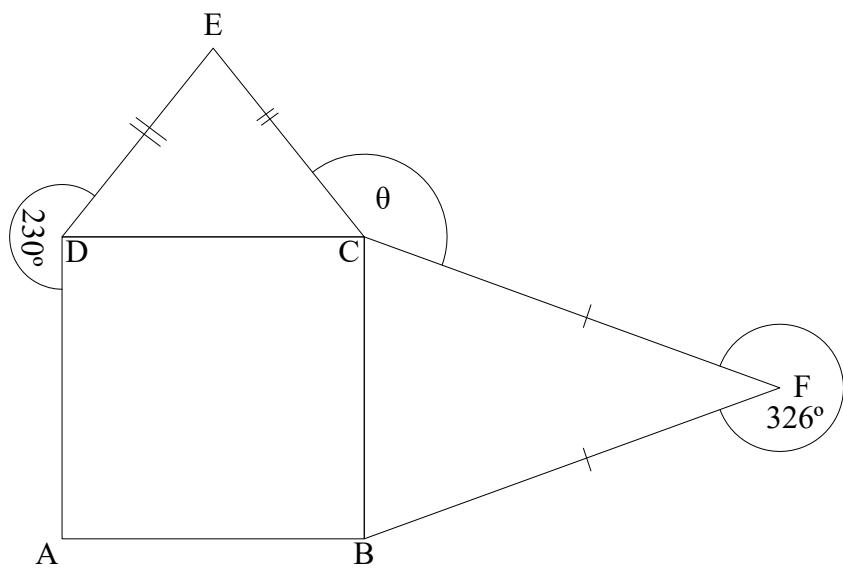


**Q11** ABCD is a square.

DCE and BCF are both isosceles triangles.

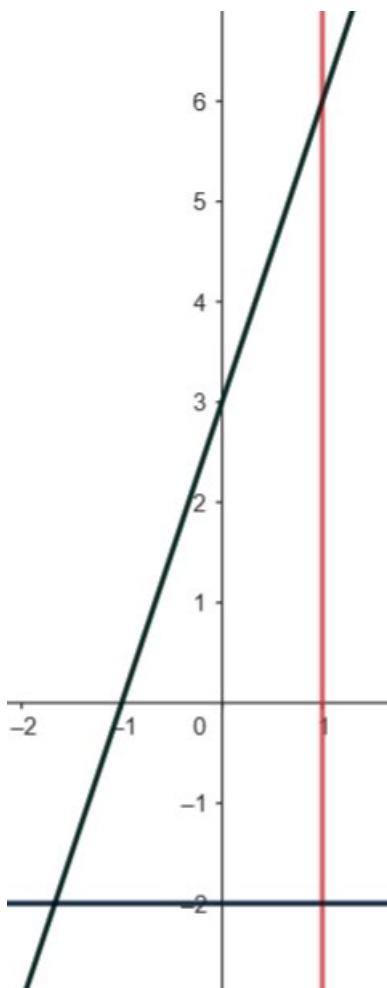
Find the value of  $\theta$ .

Give reasons.



**Q12** The lines  $y=3x+3$ ,  $y=-2$  and  $x=1$  form a triangle.

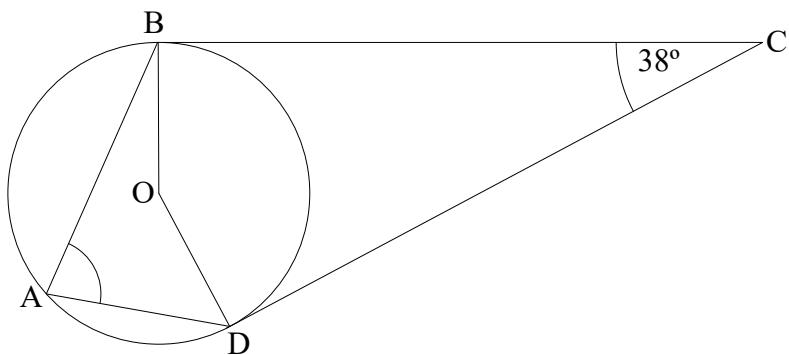
What is the area of the triangle?



**Q13** BC and CD are tangents to the circle centred at O.

Angle BCD =  $38^\circ$ .

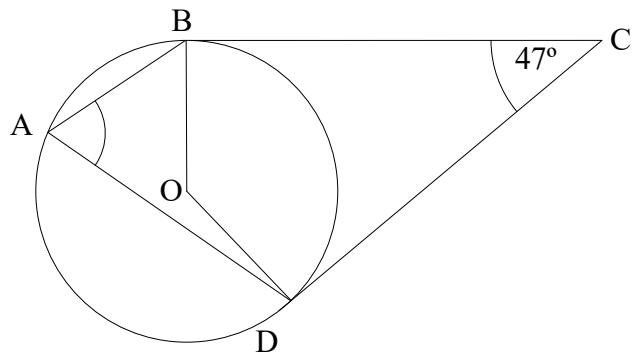
Giving reasons for each stage of your calculation, find angle DAB.



**Q14** BC and CD are tangents to the circle centred at O.

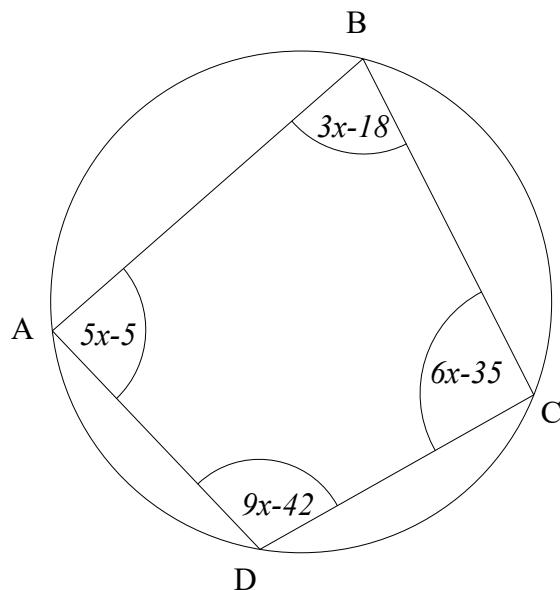
Angle BCD =  $47^\circ$ .

Giving reasons for each stage of your calculation, find angle DAB.



**Q15** Find the value of  $x$  and hence, the size of each angle in the quadrilateral below.

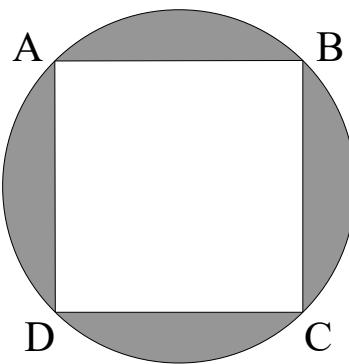
Give reasons where required.



Q16 ABCD is a square whose sides are 5cm long.

Calculate the area of the shaded part of the circle.

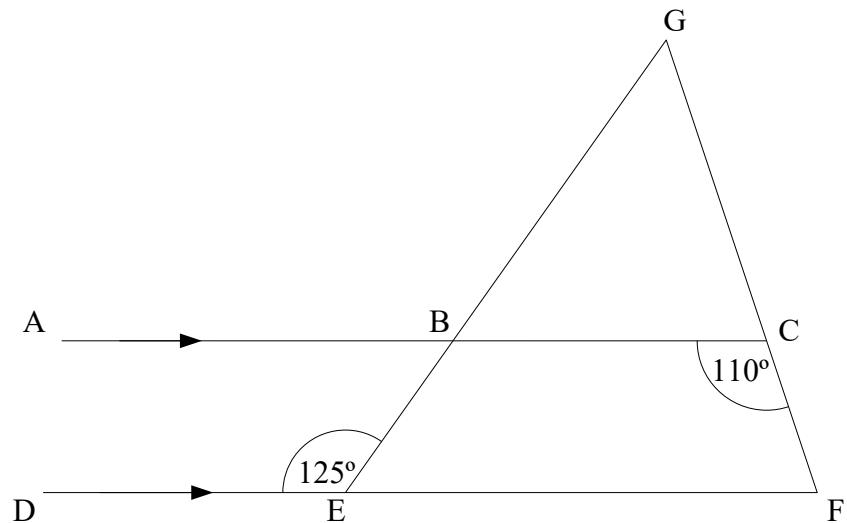
Give your answer correct to four significant figures.



**Q17** GBE and GCF are straight lines.

AC and DF are parallel straight lines.

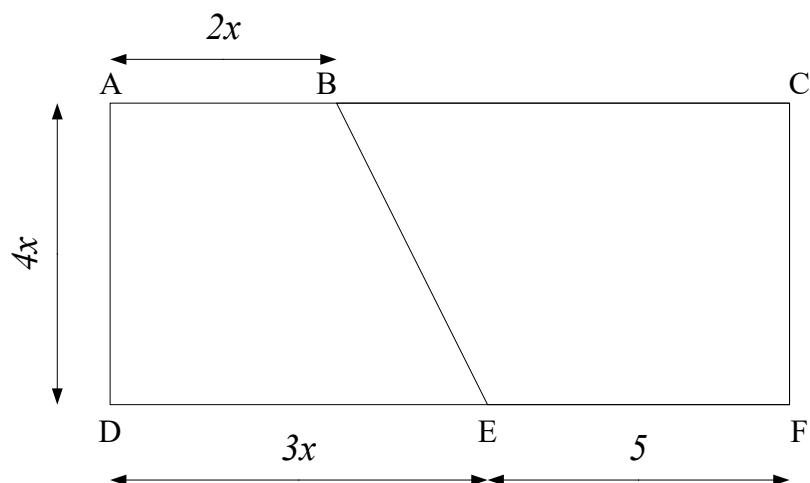
Show that triangle BGC is isosceles.



**Q18** ACDF is an oblong.

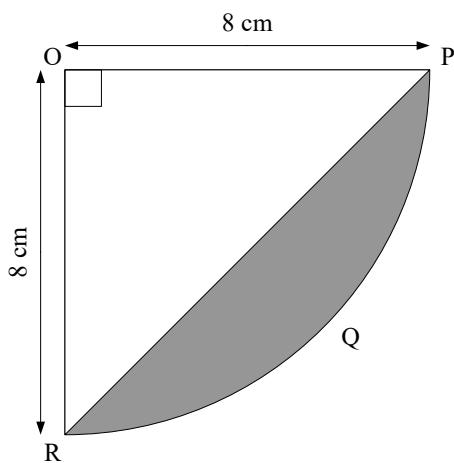
BE is a straight line.

CBEF is a trapezium with area A.



Show that  $A = 2x^2 + 20x$

**Q19** The diagram shows a sector OPQR of a circle, centre O and radius 8cm.



OPR is a triangle.

Work out the area of the shaded segment, PQR.

Give your answer to 3 significant figures.